









Robust Primary Frequency Control in Stand-alone Microgrids with High Penetration of Renewable Energy : Synthesis and Robustness Analysis

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## Outline

- Context of the study
- Microgrid description, coordinated strategy & choice of energy storage technology
- Modeling & design for  $H_{\infty}$  control
- Robustness analysis
- Numerical simulation results
- Conclusions & future work





#### Concept



# Concept of microgrids

- Integrating distributed energy resources into power systems
- Global reliability to be enhanced, reduction of carbon footprint, all with smaller investment costs





Operation



# Reliable operation of microgrids

Design of special protection schemes & control systems



Control challenges



# Main control challenges

- Stability issues
- Problems related to low inertia & uncertainties due to presence of RES
- Stand-alone mode of operation : frequency & voltage deviations within a small range are required



Microgrid. Source : <u>http://www.cleanspark.com</u>



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#### Control methods

- Proportional-integral-derivative (PID) control : limited possibility to ensure satisfactory trade-off among dynamic performances
- Fuzzy logic control : difficult to obtain a model serving for a systematic control design
- $H_{\infty}$  control : able to handle multiple requirements in a systematic manner





# Frequency stability problem of microgrids

- Frequency stability problem of microgrids with a high rate of decentralized, renewable and intermittent production
- Role of storage units
  - Fast dynamics, capacity to provide power peaks
  - Reducing frequency deviation
- Research work
  - Systematic design procedure for computing a multi-variable  $H_{\infty}$  robust controller for primary frequency regulation
  - How closed-loop operation demands must at their turn be taken into account in the initial microgrid setup & sizing







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Description



# Microgrid description

• Operating in stand-alone mode



Block diagram of the studied microgrid



Microgrid Modeling & design Analysis Results

Description



# Microgrid description

• Energy storage system



Full electrical scheme of the energy storage system

• Equation expressing the microgrid frequency deviation

$$\frac{d\Delta f_{grid}}{dt} = \frac{1}{2\underline{H}} \left[ \underline{i_{s_e} \Delta v_{sc}} + \left( \underline{v_{sc_e}} - 2\underline{R_{sc}}\underline{i_{s_e}} \right) \underline{\Delta i_s} + \underline{\Delta P_{diesel}} - \underline{\Delta P_{load}} \right] - \frac{\underline{D_{load}}}{2\underline{H}} \underline{\Delta f_{grid}} (\Delta P_{PV} = \mathbf{0})$$



Microgrid Modeling & design Analysis



# Coordinated strategy

 Proposed coordinated strategy : participation of both the storage system & the diesel generator in primary frequency control

Coordinated strategy

- Role of the storage system : to improve dynamic performances in case of disturbances
- Template for the frequency variation





Coordinated strategy

Microgrid Modeling & design Analysis

#### Coordinated strategy



Another control objective
 to regulate the DC-bus
 voltage v<sub>dc</sub> at the desired
 value of 1000 V

Performance specification on the DCbus voltage variation in response to a load step in the time domain







# Choice of energy storage technology

• Diesel power variation in the frequency domain

$$\underline{\Delta P_{diesel}}(s) = -\underbrace{\frac{1}{\underbrace{T_{diesel}s + 1}}}_{\substack{\text{Simplified dynamic}\\\text{modeling}}}\underbrace{\left(\underbrace{K_p}_{s} + \frac{K_i}{s}\right)}_{\substack{\text{Pl controller for}\\\text{frequency control}}}\underline{\Delta f_{grid}}(s), \qquad \underline{K_p} = \frac{1}{\underbrace{S_{diesel}}}$$

• Frequency deviation in the frequency domain without storage device

$$\underline{\Delta f_{grid}}(s) = \frac{1}{\underline{2Hs} + \underline{D_{load}}} \left[ \underline{\Delta P_{diesel}}(s) + \underline{\Delta P_{PV}}(s) - \underline{\Delta P_{load}}(s) \right]$$

 $\underline{\Delta P_{diff}}(s) = \underline{\Delta P_{PV}}(s) - \underline{\Delta P_{load}}(s)$ 

• Transfer function between frequency deviation & power variation

$$\Delta f_{grid}(s) = (T_{diesel}s + 1)s$$

$$\Delta P_{diff}(s) = (2HT_{diesel})s^{3} + (2H + T_{diesel}D_{load})s^{2} + (D_{load} + K_{p})s + K_{i}$$
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Choice of energy storage technology



Choice of energy storage technology



Bode diagram of the transfer function of the system

Selected frequency interval f<sub>c</sub> ∈ [0.02, 1.31] Hz for primary control participation of the storage device. Supercapacitor storage technology with its own frequency f<sub>p</sub> ∈ [0.00278, 27.78] Hz is the most appropriate

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#### Modeling for $H_{\infty}$ control

![](_page_15_Picture_2.jpeg)

# Modeling for $H_{\infty}$ control

• Modeling methodology

![](_page_15_Figure_5.jpeg)

Per-unitization system Base values for AC-side quantities  $v_{d,b} = v_{q,b} = v_b = \sqrt{3}v_r = v_{rd}$  $i_{d,b} = i_{q,b} = i_b = \frac{S_b}{v_b}$  $Z_b = \frac{v_b}{i_b}, C_b = \frac{\mathbf{1}}{Z_b \omega_b}, L_b = \frac{Z_b}{\omega_b}$  $\omega_b = \omega_0 = \omega_{grid_e} f_b = f_0 = f_{grid_e}$ Base values for DC-side quantities  $v_{b-dc} = v_{b} i_{b-dc} = \frac{S_b}{v_{b-dc}} = i_b$  $Z_{b-dc} = \frac{v_{b-dc}}{i_{b-dc}} = Z_{b} C_{b-dc} = \frac{1}{Z_{b-dc}} = C_{b}$  $L_{b-dc} = \frac{Z_{b-dc}}{\omega_b} = L_b$ 

#### Modeling for $H_{\infty}$ control

![](_page_16_Picture_2.jpeg)

![](_page_16_Picture_3.jpeg)

# Modeling for $H_{\infty}$ control

- Linear averaged model of the storage system in a per-unit term
  - $\frac{1}{\omega_b} \frac{d\Delta v_{sc}}{dt} = \frac{1}{\frac{\Delta i_s}{C_{sc}}} \frac{1}{R_{sc_p} C_{sc}} \frac{\Delta v_{sc}}{\Delta v_{sc}}$  $\frac{\mathbf{1}}{\omega_{b}} \frac{d\Delta v_{dc}}{dt} = \frac{\mathbf{1}}{C_{dc}} \alpha_{c_{e}} \Delta i_{s} + \frac{\mathbf{1}}{C_{\underline{dc}}} \underline{i_{s_{e}}} \Delta \alpha_{c}$  $-\frac{\mathbf{1}}{C_{dc}} \Big( \beta_{d_e} \underline{\Delta i_{rd}} + \underline{i_{rd_e}} \Delta \beta_d + \beta_{q_e} \underline{\Delta i_{rq}} + \underline{i_{rq_e}} \Delta \beta_q \Big) - \frac{\mathbf{1}}{R_{dc} C_{dc}} \underline{\Delta v_{dc}}$  $\frac{\mathbf{1}}{\omega_{b}}\frac{d\Delta i_{s}}{dt} = \frac{\mathbf{1}}{L_{c}}\frac{\Delta v_{sc}}{L_{c}} - \frac{\underline{R_{sc}} + \underline{R_{c}}}{L_{c}}\underline{\Delta i_{s}} - \frac{\mathbf{1}}{L_{c}}\alpha_{c_{e}}\underline{\Delta v_{dc}} - \frac{\mathbf{1}}{L_{c}}\frac{v_{dc_{e}}}{\Delta \alpha_{c}}\Delta \alpha_{c}$  $\frac{\mathbf{1}}{\omega_{h}} \frac{d\Delta i_{rd}}{dt} = \frac{\mathbf{1}}{L_{f}} \beta_{d_{e}} \underline{\Delta v_{dc}} + \frac{\mathbf{1}}{L_{f}} \underline{v_{dc_{e}}} \Delta \beta_{d} - \frac{R_{f}}{L_{f}} \underline{\Delta i_{rd}} + \underline{\omega_{grid_{e}}} \Delta i_{rq} + \underline{i_{rq_{e}}} \Delta \omega_{grid}$  $\frac{1}{\omega_{h}}\frac{d\Delta i_{rq}}{dt} = \frac{1}{L_{f}}\beta_{q_{e}}\Delta v_{dc} + \frac{1}{L_{f}}\frac{v_{dc_{e}}}{\omega_{dc_{e}}}\Delta\beta_{q} - \frac{R_{f}}{L_{f}}\Delta i_{rq} - \frac{\omega_{grid_{e}}}{\omega_{grid_{e}}}\Delta i_{rd} - \frac{i_{rd_{e}}}{\omega_{grid_{e}}}\Delta\omega_{grid}$

ogrid Modeling & design Analysis

![](_page_17_Picture_2.jpeg)

# Modeling for $H_{\infty}$ control

• Power variation of diesel generation in the time domain for only primary control participation

$$\frac{d\Delta P_{diesel}}{dt} = -\frac{\mathbf{1}}{T_{diesel}} \frac{\Delta P_{diesel}}{-\frac{\mathbf{1}}{T_{diesel}} \frac{\Delta f_{grid}}{-\frac{\mathbf{1}}{T_{diesel}} \frac{-$$

• Linear averaged model in the state-space form for  $H_{\infty}$  control

 $\begin{cases} \underline{\Delta \dot{\mathbf{x}}} = \mathbf{A}\underline{\Delta \mathbf{x}} + \mathbf{B}_{1}\underline{\Delta \mathbf{u}} + \mathbf{B}_{2}\underline{\Delta \mathbf{w}} \\ \underline{\Delta \mathbf{y}} = \mathbf{C}\underline{\Delta \mathbf{x}} + \mathbf{D}_{1}\underline{\Delta \mathbf{u}} + \mathbf{D}_{2}\underline{\Delta \mathbf{w}} \end{cases}$ 

$$\underline{\Delta \mathbf{x}} = \left[ \underbrace{\Delta v_{dc}}_{\Delta v_{dc}} \underline{\Delta P_{diesel}}_{\Delta f_{grid}} \right]^{T} : \text{ state vector}$$

$$\underline{\Delta \mathbf{u}} = \left[\underline{\Delta i_s^{ref}} \ \underline{\Delta i_{rd}^{ref}}\right]^T : \text{ control input vector } (\Delta i_{rq}^{ref} = \mathbf{0})$$

 $\underline{\Delta \mathbf{w}} = \underline{\Delta P_{load}}$  : disturbance input

 $\Delta \mathbf{y} = \begin{bmatrix} \Delta \mathbf{v}_{dc} & \Delta f_{grid} \end{bmatrix}^T$ : measured output vector

rogrid Modeling & design Analysis Results

Modeling for  $H_{\infty}$  control

![](_page_18_Picture_2.jpeg)

#### Modeling for $H_{\infty}$ control

![](_page_18_Figure_4.jpeg)

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![](_page_19_Picture_1.jpeg)

#### $H_{\infty}$ control design

![](_page_19_Picture_3.jpeg)

 $H_{\infty}$  control design

#### Proposed global control structure

Active power variation calculation of the storage system

![](_page_19_Figure_6.jpeg)

![](_page_20_Picture_2.jpeg)

#### $H_{\infty}$ control design

![](_page_20_Figure_4.jpeg)

Control configuration in the so-called  $\mathbf{P}$  –  $\mathbf{K}$  form

- $H_{\infty}$  control level
  - > Model associated with  $H_{\infty}$  control
    - ✓ Plant "P"
      - Linear state-space model **G**(*s*) Weighting functions
    - ✓  $H_{\infty}$  controller **K**(*s*)

$$\underline{\Delta \mathbf{u}} = \begin{bmatrix} \Delta i_s^{ref} & \Delta i_{rd}^{ref} \end{bmatrix}^T$$

$$\checkmark \quad \text{Disturbance input} \\ \underline{\Delta \mathbf{w}} = \Delta P_{load}$$

$$\underline{\Delta \mathbf{y}} = \left[\underline{\Delta v_{dc}} \ \underline{\Delta f_{grid}}\right]^T$$

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![](_page_21_Picture_1.jpeg)

![](_page_21_Picture_2.jpeg)

# $H_{\infty}$ control design

- Weighting function selection
  - DC-bus voltage variation  $\Delta v_{dc}$  & frequency variation  $\Delta f_{grid}$  are

bounded by first-order weighting functions

$$\frac{1}{W_{perf}(s)} = \frac{s + \omega_b A_{\varepsilon}}{s/M_s + \omega_b}$$

 $M_s$ : limitation of the overshoot  $\omega_b$ : the desired response time  $A_{\varepsilon}$ : limitation of the steady-state error

$$M_{s_{1}} = \frac{\Delta v_{dc_{max}}}{\underline{\Delta P_{load}}}, A_{\varepsilon_{1}} = \frac{\Delta v_{dc_{min}}}{\underline{\Delta P_{load}}}$$
$$\omega_{b_{1}} = \mathbf{1}/(\mathbf{40}T_{0_{rdq}})(t_{r_{1}} \approx \mathbf{1.2 s})$$
$$M_{s_{2}} = \frac{\Delta f_{grid_{max}}}{\underline{\Delta P_{load}}}, A_{\varepsilon_{2}} = \frac{\Delta f_{grid_{min}}}{\underline{\Delta P_{load}}}$$
$$\omega_{b_{2}} = \mathbf{1}/(\mathbf{20}T_{0_{rdq}})(t_{r_{2}} \approx \mathbf{0.6 s})$$

![](_page_21_Figure_10.jpeg)

 $H_{\infty}$  control design

![](_page_22_Picture_1.jpeg)

# $H_{\infty}$ control design

✓ Active power injection or absorption of the storage system is controlled via  $i_s$ . Storage device current reference variation  $\Delta i_s^{ref}$  is bounded by a band-pass weighting function

![](_page_22_Figure_4.jpeg)

![](_page_22_Figure_5.jpeg)

 $H_{\infty}$  control design

![](_page_23_Figure_3.jpeg)

Selected frequency interval for primary control participation :  $f_c \in [0.02, 1.31]$  Hz (or  $\omega_c \in [0.12, 8.21]$  rad/s)

 $\frac{\omega_{bc_{11}}}{A_{u_1}} = 0.12 \div 174.55, \qquad \frac{\omega_{bc_{12}}}{M_{u_1}} = 0.12 \div 174.55$ 

Own frequency of supercapacitor technology :  $f_p \in$  [0.00278, 27.78] Hz (or  $\omega_p \in$  [0.0175, 174.55] rad/s)

Own frequency of the selected supercapacitor technology :  $f_p = 0.48$  Hz (or  $\omega_p = 3.04$  rad/s)

![](_page_24_Picture_1.jpeg)

![](_page_24_Picture_2.jpeg)

#### $H_{\infty}$ control design

✓ DC-bus voltage is regulated via  $i_{rd}$ . The inverter output current reference variation in *d*-axis  $\Delta i_{rd}^{ref}$  is bounded by the first-order weighting function

![](_page_24_Figure_5.jpeg)

 $H_{\infty}$  control design

ogrid Modeling & design Analysis Results Conclusions

![](_page_25_Picture_2.jpeg)

## $H_{\infty}$ control design

- $\succ$   $H_{\infty}$  controller synthesis
  - ✓ "hinfsyn" function

![](_page_25_Picture_6.jpeg)

✓ Minimization of the norm

![](_page_25_Picture_8.jpeg)

- *S/KS* mixed-sensitivity optimization must typically be solved
- ✓ Sensitivity functions

$$S_{1} = \frac{\Delta v_{dc}}{\Delta P_{load}}, S_{2} = \frac{\Delta f_{grid}}{\Delta P_{load}}$$
$$KS_{1} = \frac{\Delta i_{s}^{ref}}{\Delta P_{load}}, KS_{2} = \frac{\Delta i_{rd}^{ref}}{\Delta P_{load}}$$

![](_page_25_Figure_12.jpeg)

![](_page_25_Picture_15.jpeg)

![](_page_26_Picture_0.jpeg)

![](_page_26_Picture_1.jpeg)

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![](_page_26_Picture_9.jpeg)

![](_page_27_Picture_0.jpeg)

![](_page_27_Picture_3.jpeg)

#### Configuration for robustness analysis

![](_page_27_Figure_5.jpeg)

![](_page_28_Picture_0.jpeg)

# Configuration for robustness analysis

 $\mathsf{Y}_\Delta$ 

 $M(s) = N_{11}(s)$ 

Configuration

Structured singular value (μ-analysis)

Modeling & design Analysis Results Conclusions

- RS & RP : the closedloop system remains stable and wellperforming for a given uncertainty level ? ▲
- Parametric uncertainties taken into account

 $\mathsf{u}_{\Delta}$ 

V<sub>SCe</sub>

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![](_page_28_Figure_5.jpeg)

 $\mathbf{K}(\mathbf{s})$ 

Configuration for robustness analysis

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Ν

![](_page_29_Picture_0.jpeg)

![](_page_29_Picture_3.jpeg)

#### $\mu$ -analysis results

• Condition for robust performance  $\mu \leq 1$  is verified for the uncertainty of up to  $\pm 69\%$  of the rated value of

![](_page_29_Figure_6.jpeg)

![](_page_30_Picture_0.jpeg)

![](_page_30_Picture_1.jpeg)

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![](_page_30_Picture_9.jpeg)

![](_page_31_Picture_0.jpeg)

![](_page_31_Picture_2.jpeg)

## Numerical simulation results

- Non-linear averaged model is used for the time-domain simulations
- Taking into account SoC of the supercapacitor ( $v_{sc}$  is considered as a state variable) in simulation
- Load profile is varied in step of + 5% of the rated load power (60 kW) at t = 1 s, -5% at t = 9 s, -5% at t = 17 s and +5% at t = 25 s

![](_page_31_Picture_7.jpeg)

![](_page_32_Picture_0.jpeg)

![](_page_32_Picture_2.jpeg)

# Numerical simulation results

• Desired time-domain performance corresponding to the parameter choice of the weighting function  $W_{perf_2}(s)$  is well-respected

![](_page_32_Figure_5.jpeg)

Time-domain response of the microgrid frequency  $f_{grid}$  under small step load disturbances of ± 5% of the rated load power (± 60 kW) from the rated parameters

![](_page_33_Picture_0.jpeg)

• DC-bus voltage control objective is satisfied with respect to the parameter selection of the weighting function  $W_{perf_1}(s) \longrightarrow H_{\infty}$  controller ensures desired performances

![](_page_33_Figure_2.jpeg)

![](_page_34_Picture_0.jpeg)

![](_page_34_Picture_2.jpeg)

#### Numerical simulation results

- $SoC_e \in [0.25, 1] (v_{SC_e} \in [390 V, 780 V])$
- Desired overshoot is well-respected irrespective of the initial value of *SoC*

![](_page_34_Figure_6.jpeg)

Time-domain response of the microgrid frequency  $f_{grid}$  under small step load disturbances of ± 5% of the rated load power (± 60 kW) taking into account the uncertainty on  $SoC_e$  (or  $v_{sc_e}$ )

![](_page_35_Picture_0.jpeg)

![](_page_35_Picture_2.jpeg)

#### Numerical simulation results

• Overshoot of the DC-bus voltage is satisfied irrespective of the initial value of *SoC* 

![](_page_35_Figure_5.jpeg)

![](_page_35_Figure_6.jpeg)

Time-domain response of the DC-bus voltage  $v_{dc}$  under small step load disturbances of  $\pm$  5% of the rated load power ( $\pm$  60 kW) taking into account the uncertainty on SoC<sub>e</sub> (or  $v_{sc_e}$ )

![](_page_36_Picture_0.jpeg)

![](_page_36_Picture_1.jpeg)

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![](_page_36_Picture_9.jpeg)

![](_page_37_Picture_1.jpeg)

![](_page_37_Picture_2.jpeg)

## Conclusions & future work

- Conclusions
  - ➤ Systematic design procedure for computing a multi-variable H<sub>∞</sub> robust controller for primary frequency regulation in stand-alone microgrids highly penetrated by renewable energy sources
  - Effectiveness of the proposed  $H_{\infty}$  robust control strategy has been validated via numerical simulation results
  - Robustness analysis of the synthesized  $H_{\infty}$  controller taking into account the uncertainty on  $SoC_e$  of the supercapacitor
- Future work
  - Design of a robust control strategy for PCC voltage regulation
  - Practical implementation of the proposed control algorithms on a realtime test bench

![](_page_37_Picture_11.jpeg)

![](_page_38_Picture_0.jpeg)

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![](_page_38_Picture_1.jpeg)

G2E Lab

gipsa-lab

# Questions ???

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![](_page_38_Picture_3.jpeg)