H_{∞} Multi-objective and Multi-Model MIMO control design for Broadband noise attenuation in a 3D enclosure

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Introduction

- General context
- PhD objective
- State of Art
- Scope of the presentation

2 System to control

- **3** Control Strategy
- 4 Results
- **5** Conclusions and Perspectives



Duct



Feedforward + feedback

Headphone





SISO control

Co-located actuator and sensor



SISO control
Co-located actuator and sensor

General Context Active Noise Control (ANC) in a cavity



Characteristics of ANC in a cavity

- Stationary waves
- Actuators and sensors co-located or not
- feedback or feedback + feedforward
- d narrow or broadband noise
- SISO or MIMO control

PhD objective Active control of broadband low frequency noise in car cabin



PhD objective Active Noise Control of broadband noise





ANC problem characteristics

- 3D enclosure
- Actuators and sensors not co-located
- No measure of w is available
- d broadband low frequency noise

Limitations involved

- Waterbed effect (Bode integral)
 - Non minimum phase zeros



Fig. 2 – Control scheme for attenuation of interior noise in automobiles. Accelerometers attached to the bodywork provide reference signals for multiple-channel adaptive feedforward control.

¹T. Sutton, S. J. Elliott, M. McDonald, *et al.*, "Active control of road noise inside vehicles", *Noise Control Engineering Journal*, vol. 42, no. 4, pp. 137–147, 1994.

State of Art Internal Model Control (feedback)



Figure 5.2: Mutli-input, multi-output feedback control system in the rectangular enclosure. 2

²J. Cheer, "Active control of the acoustic environment in an automobile cabin", PhD thesis, University of Southampton, Southampton, 2012, p. 346.

Scope of the presentation



Problem

- Attenuate broadband low frequency noise;
- In a closed cavity;
- by feedback.

Goal of the presentation

Compare SISO and MIMO achievable performances.

Content

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2 System to control

- Experimental Set up
- Identification

3 Control Strategy

- Control problem formulation
- Multi-objective optimization
- Controller Structure
- Initialization

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Experimental set up



MIMO Identification

Frequency Domain, Continuous time model



Fit indicator

	LS ₁	LS ₂	LS ₃
M ₁	86.2326	84.1038	91.1196
M ₂	84.6231	88.8484	91.1542

Remark: SISO transfers contain RHP zeros.



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Control problem formulation



subject to $\begin{cases} \left\| W_2 T_{W \to u_j} \right\|_{\infty} < 1 \\ \left\| W_3 T_{d'_j \to e_j} \right\|_{\infty} < 1 \\ |\rho_{i_K}| < f_e/N \\ Re(\rho_{i_K}) < 0 \end{cases}$ **Optimization problem** $\min_{K} \left\| W_1 T_{w \to e_1} \right\|_{\infty}$

Control problem formulation Additional robustness needed

Environment conditions modify acoustic transfers



A multi-model approach was used to tackle system variations

Control problem formulation



Optimization problem

$$\min_{K} \max_{1,...,N} \left\| W_1 T_{w \to e_1} \right\|_{\infty} \quad \text{subject to} \quad \begin{cases} \max_{1,...,N} \left\| W_2 T_{w \to u_i} \right\|_{\infty} < 1 \\ \max_{1,...,N} \left\| W_3 T_{d'_j \to e_i} \right\|_{\infty} < 1 \\ |\rho_{i_K}| < f_e/N \\ Re(\rho_{i_K}) < 0 \end{cases}$$

Multi-objective and Multi-model optimization

Motivations

- Be able to consider various constraints without pessimism;
- Clearly distinguish objective and constraints;
- Have the possibility to mix H_2 and H_∞ objectives, if needed;
- Be able to structure the controller;
- Be able to consider reduce order controller.

Optimization tool: systune

- Specialized in tuning fixed-structure control systems;
- Based on non smooth optimization;
- P. Apkarian, "Tuning controllers against multiple design requirements", in *American Control Conference (ACC)*, Washington, 2013, pp. 3888–3893

Drawback

- May lead to local optima;
- Necessity of "good" initialization and controller structure.

Controller Structure

State feedback observer

Model of the system

- No real time measure of w
- ► G_p is known

$$\begin{cases} \dot{x} = Ax + B_u u + B_w w\\ e = Cx + D_u u + D_w w\end{cases}$$

 $\label{eq:model} \left\{ \begin{array}{l} \dot{\hat{x}} = A \hat{x} + B_u u + {\sf K}_{\sf f} \left(e - \hat{e} \right) \\ u = - {\sf K}_{\sf c} \hat{x} \end{array} \right.$



LQ criteria

$$J_{LQ} = \min_{K_c} \|W_{LQ}e\|_2^2 + \rho \|u\|_2^2$$

- \triangleright W_{LQ} is a bandpass filter (attenuation frequency range)
- \triangleright ρ manages trade-off between performances and control energy

Kalman filter

$$\begin{cases} \dot{x}_a = A_a x_a + B_{u_a} u + B_{w_a} w \\ e = C_a x_a + D_{u_a} u + D_{w_a} w + v \end{cases}$$

Tuning parameters are the covariances of noises v and w

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Results Narrow attenuation: [190-220] Hz



Results <u>Narrow attenuation:</u> [190-300] Hz



Results Experimentation: 190-300 Hz (MIMO)



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Conclusions and Perspectives

Conclusions

- A general framework (for identification and control) was presented;
- It allows to quantify and compare SISO and MIMO achievable performances according to :
 - Frequency range of attenuation ;
 - Actuators and sensors position ;
 - Cavity geometry
 - ...

Ongoing work

- Compare feedback and feedforward control
- Apply methodology to the industrial problem where:
 - G_p is unknown
 - System order and dimensions are higher