

Toward nonlinear tracking and rejection using LPV control

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Fondation EADS

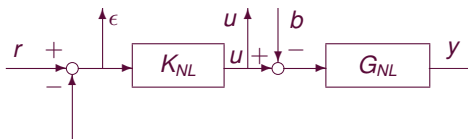


International Workshop on Robust LPV Control Techniques and
Anti-Windup Design

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A typical control problem

- Usual control problems involve both tracking and rejection specifications
- Let us focus on a simple problem: Given a nonlinear plant G_{NL} , find K_{NL} such that



- Typical control specs
 - tracking of step references with a null static error and a response time \leq a given time (e.g. 0.1 s)
 - rejection of step disturbances at the plant input
 - limited control energy

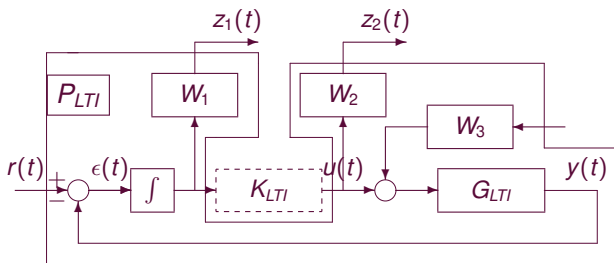
- LTI case: H_∞ control achieves tracking and rejection specs
- NL case: the usually proposed extension is \mathcal{L}_2 gain control
- \mathcal{L}_2 gain nonlinear controller can be computed using LPV approach

Does the (LPV/nonlinear) \mathcal{L}_2 gain controller achieves tracking and rejection?

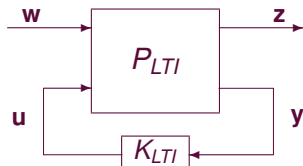
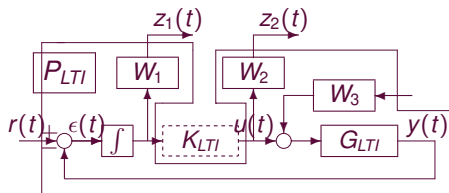
Typical approach for LTI plant and controller

LTI case: H_∞ control approach

- With weighting functions W_1 , W_2 , W_3 suitable for the specs
- Compute K_{LTI} such that H_∞ norm of the following closed loop system less than 1



H_∞ control approach (recall)



Given an (augmented) LTI plant P_{LTI}

$$\begin{cases} \dot{x}(t) = Ax(t) + B_w w(t) + B_u u(t) \\ z(t) = C_z x(t) + D_{zw} w(t) + D_{zu} u(t) \\ y(t) = C_y x(t) + D_{yw} w(t) + D_{yu} u(t) \end{cases}$$

Compute an LTI controller K_{LTI}

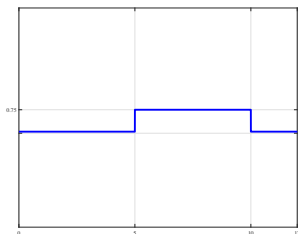
$$\begin{cases} \dot{\bar{x}}(t) = A_K \bar{x}(t) + B_K y(t) \\ u(t) = C_K \bar{x}(t) \end{cases}$$

Such that

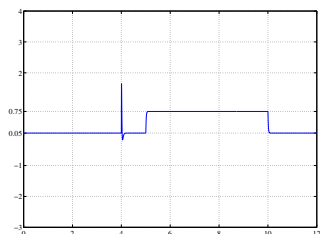
$$\|T_{w \rightarrow z}\|_\infty \leq 1$$

- Efficient solution (Riccati or LMI)

Comments on the result: step disturbance at 4s and square reference



Reference



Output

■ Nice steady state behaviour

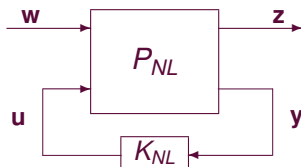
- Stability of LTI system \Rightarrow for constant input, output \rightarrow constant
- Stability + integral control \Rightarrow null error

■ Nice transient behavior

- Inequality on the weighted H_∞ norm of the closed loop system

- LTI case: H_∞ control achieves tracking and rejection specs
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Does the (LPV/nonlinear) \mathcal{L}_2 gain controller achieves tracking and rejection?



Given an (augmented) nonlinear plant P_{NL}

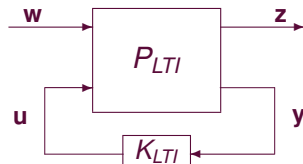
$$\begin{cases} \dot{x}(t) = f(x(t), w(t), u(t)) \\ z(t) = g(x(t), w(t), u(t)) \\ y(t) = h(x(t), w(t)) \end{cases}$$

Compute a nonlinear controller K_{NL}

$$\begin{cases} \dot{\bar{x}}(t) = f_K(\bar{x}(t), y(t)) \\ u(t) = g_K(\bar{x}(t), y(t)) \end{cases}$$

such that the \mathcal{L}_2 gain of the closed loop system is less than 1: for all w

$$\forall T > 0, \int_0^T z(t)^T z(t) dt \leq \int_0^T w(t)^T w(t) dt$$



- For LTI system, $\|T_{w \rightarrow z}\|_\infty \leq 1$ is equivalent to the \mathcal{L}_2 gain is less than 1: for all w

$$\forall T > 0, \int_0^T z(t)^T z(t) dt \leq \int_0^T w(t)^T w(t) dt$$

- A natural idea: extend the H_∞ control to nonlinear systems by the \mathcal{L}_2 gain control: usually referred to as “nonlinear H_∞ control”

Two questions

- 1 How to compute a solution (nonlinear controller) to the \mathcal{L}_2 gain control problem?

No efficient direct approach \Rightarrow indirect approach: Quasi LPV control

- 2 Does the \mathcal{L}_2 gain controller ensures nice tracking and rejection properties as in the LTI case?

See application on the illustrative example

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See application on the illustrative example

Given a Linear Parameter Varying (LPV) plant G_{LPV}

$$\begin{cases} \dot{x}(t) &= \mathbf{A}(\theta(t))x(t) &+ \mathbf{B}_1(\theta(t))w(t) &+ \mathbf{B}_2(\theta(t))u(t) \\ z(t) &= \mathbf{C}_1(\theta(t))x(t) &+ \mathbf{D}_{11}(\theta(t))w(t) &+ \mathbf{D}_{12}(\theta(t))u(t) \\ y(t) &= \mathbf{C}_2(\theta(t))x(t) &+ \mathbf{D}_{21}(\theta(t))w(t) &+ \mathbf{D}_{22}(\theta(t))u(t) \end{cases}$$

- $\theta(t)$ = vector of time varying parameters, measured in real-time, which belong to a given interval
- $\mathbf{A}(\cdot)$, $\mathbf{B}_1(\cdot)$, ... rational functions of $\theta_i(t)$

Compute an LPV controller K_{LPV}

$$\begin{cases} \dot{\bar{x}}(t) &= \mathbf{A}_K(\theta(t))\bar{x}(t) &+ \mathbf{B}_K(\theta(t))y(t) \\ u(t) &= \mathbf{C}_K(\theta(t))\bar{x}(t) \end{cases}$$

Such that the \mathcal{L}_2 gain of the closed loop system is less than 1: for all w

$$\forall T > 0, \int_0^T z(t)^T z(t) dt \leq \int_0^T w(t)^T w(t) dt$$

- Solutions of the LPV control problem can be computed using LMI optimization
- A strong motivation of the LPV control problem is to propose, in contrast with the gain scheduling control, a rigorous solution to the nonlinear \mathcal{L}_2 gain control problem¹

¹W. J. Rugh and J. S. Shamma, "Research on gain scheduling," *Automatica*, vol. 36, pp. 1401–1425, 2000.

To the (augmented) nonlinear plant P_{NL}

$$\begin{cases} \dot{x}(t) &= f(x(t), w(t), u(t)) \\ z(t) &= g(x(t), w(t), u(t)) \\ y(t) &= h(x(t), w(t)) \end{cases} \quad (1)$$

is associated an LPV plant P_{LPV}

$$\begin{cases} \dot{x}(t) &= \mathbf{A}(\theta(t))x(t) &+ \mathbf{B}_1(\theta(t))w(t) &+ \mathbf{B}_2(\theta(t))u(t) \\ z(t) &= \mathbf{C}_1(\theta(t))x(t) &+ \mathbf{D}_{11}(\theta(t))w(t) &+ \mathbf{D}_{12}(\theta(t))u(t) \\ y(t) &= \mathbf{C}_2(\theta(t))x(t) &+ \mathbf{D}_{21}(\theta(t))w(t) &+ \mathbf{D}_{22}(\theta(t))u(t) \end{cases} \quad (2)$$

such that with

$$\Omega_{NL} = \{ (x \ z \ y \ w \ u) \mid (1) \text{ is satisfied} \}$$

and

$$\Omega_{LPV} = \{ (x \ z \ y \ w \ u) \mid (2) \text{ is satisfied} \}$$

we have

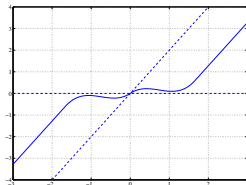
$$\Omega_{NL} \subset \Omega_{LPV}$$

A Nonlinear plant as an illustrative example

$y = G_{NL}(u)$ with

$$\begin{cases} \dot{x}_1(t) &= -100\varphi(x_1(t)) - 70x_2(t) + 300u(t) \\ \dot{x}_2(t) &= 70x_1(t) - 14x_2(t) \\ y(t) &= x_1(t) \end{cases}$$

with φ defined by



that is

$$0 \leq \varphi(x_1) \leq 2x_1$$

To the nonlinear plant G_{NL} :

$$\begin{cases} \dot{x}_1(t) &= -100\varphi(x_1(t)) - 70x_2(t) + 300u(t) \\ \dot{x}_2(t) &= 70x_1(t) - 14x_2(t) \\ y(t) &= x_1(t) \end{cases}$$

we associate the LPV plant G_{LPV} :

$$\begin{cases} \dot{x}(t) &= A_G(\theta(t))x(t) + \begin{bmatrix} 300 \\ 0 \end{bmatrix} u(t) \\ y(t) &= \begin{bmatrix} 1 & 0 \end{bmatrix} x(t) \end{cases}, \quad \theta(t) \in [0, 2]$$

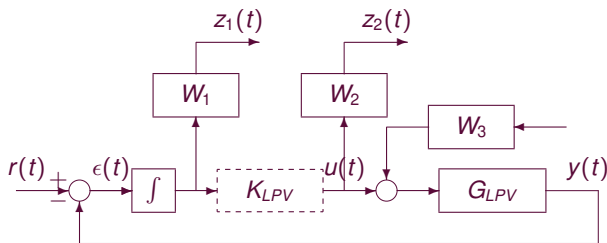
with²

$$A_G(\theta(t)) = \begin{bmatrix} 0 & -70 \\ 70 & -14 \end{bmatrix} + \theta(t) \begin{bmatrix} -100 & 0 \\ 0 & 0 \end{bmatrix}$$

² $\theta(t) = \frac{\varphi(y(t))}{y(t)}$ with $0 \leq \varphi(y) \leq 2y$

Application to the illustrative example of the quasi LPV method

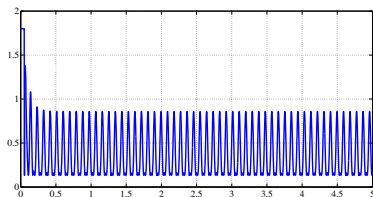
- For step tracking and step rejection, an LPV controller is computed using the augmented plant defined as follows.



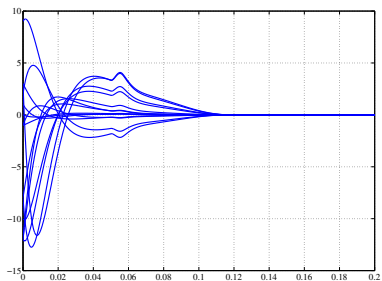
- Thanks to the embedding process, this controller is a solution to the nonlinear \mathcal{L}_2 gain control problem
- Does the LPV controller ensure satisfying tracking and rejection?

Behaviour of the **LPV** closed loop system with respect to initial conditions & zero inputs

For a given function $\theta(t) \in [0, 2]$

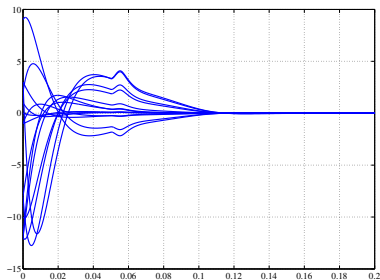


Output $y(t)$ for different initial conditions x_0



Behaviour of the **LPV** closed loop system with respect to initial conditions & zero inputs

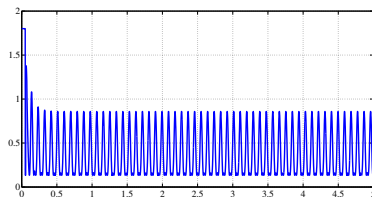
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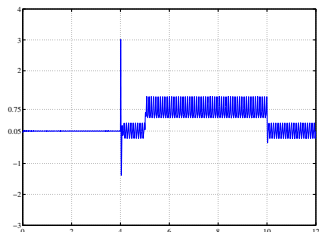
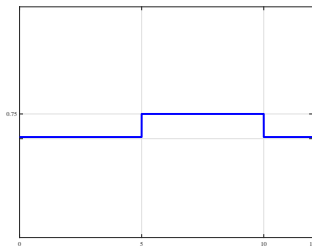
(\mathcal{L}_2 gain) stability ensures convergence to 0 for different initial conditions

Behaviour of the LPV closed loop system with respect to step reference & disturbance

For a given function $\theta(t) \in [0, 2]$

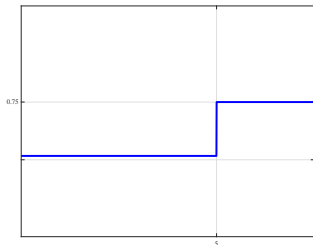


Output $y(t)$ for $x_0 = 0$, a step disturbance at 4s and a square reference signal

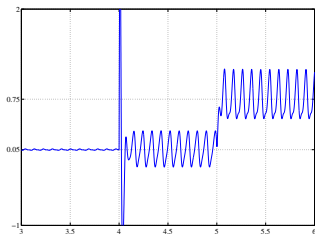


Behaviour of the LPV closed loop system with respect to step reference & disturbance

Output $y(t)$ for $x_0 = 0$, a step disturbance at 4s and a square reference signal



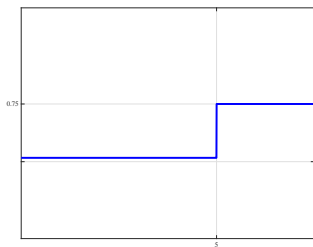
Reference



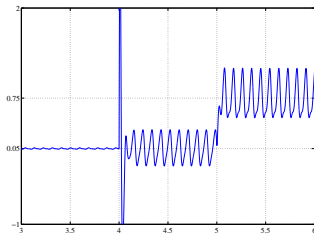
Output

Behaviour of the LPV closed loop system with respect to step reference & disturbance

Output $y(t)$ for $x_0 = 0$, a step disturbance at 4s and a square reference signal



Reference



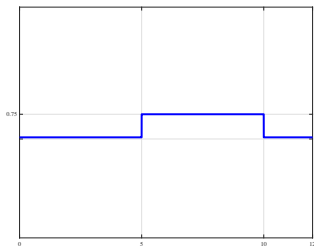
Output

(\mathcal{L}_2 gain) stability + integral control do not ensure step tracking/rejection for LPV system

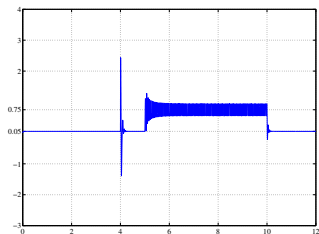
Behaviour of the **non-linear** closed loop system with respect to step reference & disturbance

What's going on with the non-linear plant?

Output $y(t)$ for $x_0 = 0$, a step disturbance at 4s and a square reference signal



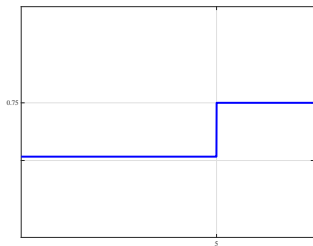
Reference



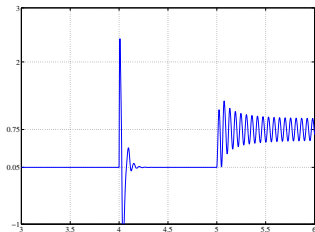
Output

Behaviour of the **non-linear** closed loop system with respect to step reference & disturbance

Output $y(t)$ for $x_0 = 0$, a step disturbance at 4s and a square reference signal



Reference



Output

$(\mathcal{L}_2 \text{ gain})$ stability + integral control do not ensure step tracking/rejection for nonlinear system

Except for input signals close to 0

- For inputs close to 0, the \mathcal{L}_2 gain control solution reduces to the H_∞ one³
- Null static errors for step reference & disturbance by integral control depend on the property that for constant inputs, the system signals tend to constant values
- Unfortunately, this property is not ensured by (\mathcal{L}_2 gain) stability

How to ensure a good behavior?

³A. J. van der Schaft, " \mathcal{L}_2 -gain analysis of nonlinear systems and nonlinear state feedback H_∞ control," *IEEE Trans. Automatic Control*, vol. 37, no. 6, pp. 770–784, June 1992

How to ensure a good behaviour? Use the \mathcal{L}_2 incremental gain

Nonlinear plant G_{NL}

$$\begin{cases} \dot{x}(t) &= f(x(t), w(t)) \\ z(t) &= g(x(t), w(t)) \end{cases}$$

- (\mathcal{L}_2 gain) stability if $\exists \gamma \geq 0, \forall w,$

$$\forall T > 0, \int_0^T z(t)^T z(t) dt \leq \gamma^2 \int_0^T w(t)^T w(t) dt$$

\mathcal{L}_2 gain of G_{NL} ($\|G_{NL}\|_{i-2}$) = the smallest value of such γ

- incremental (\mathcal{L}_2 gain) stability if stability and $\exists \eta \geq 0, \forall T > 0, \forall w_1, \forall w_2,$

$$\int_0^T (z_1(t) - z_2(t))^T (z_1(t) - z_2(t)) dt \leq \eta^2 \int_0^T (w_1(t) - w_2(t))^T (w_1(t) - w_2(t)) dt$$

Incremental \mathcal{L}_2 gain of G_{NL} ($\|G_{NL}\|_{\Delta}$) = the smallest value of such η

- For an LTI system, H_{∞} norm = \mathcal{L}_2 gain = incremental \mathcal{L}_2 gain

Why incremental (\mathcal{L}_2) gain is nice for control performance?

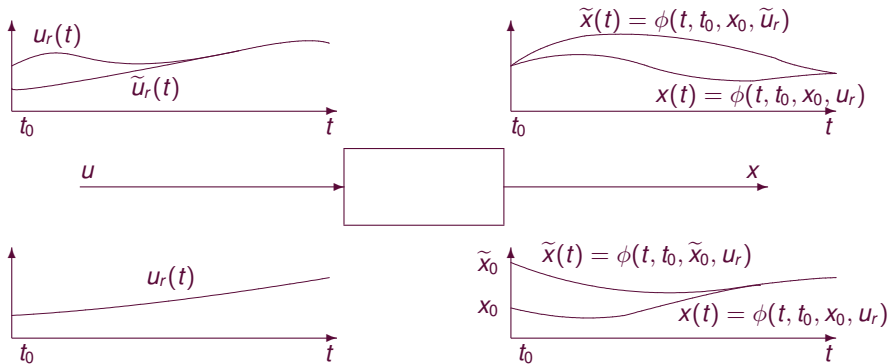
	LTI	NL	NL
↓ Specs \ Norm →	H_∞	\mathcal{L}_2 gain	incremental gain
Unique steady state	YES	NO	YES
Convergence of the unperturbed motions	YES	NO	YES
Constant input → constant output	YES	NO	YES
T periodic input → T periodic output	YES	NO	YES
Quantitative perf.	YES	NO	YES
Robustness	YES	YES	YES

V. Fromion and S. Monaco and D. Normand-Cyrot, The weighted incremental norm approach: from linear to nonlinear H_∞ control, Automatica 2001

V. Fromion and G. Scorletti. The behavior of incrementally stable discrete time systems, System and Control Letters 2002

V. Fromion, Some results on the behavior of Lipschitz continuous systems, ECC 97

Unique steady state

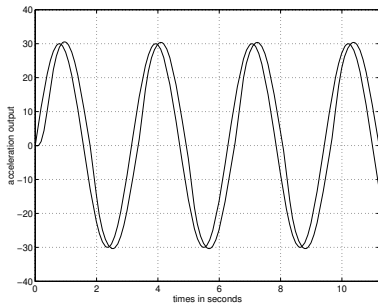
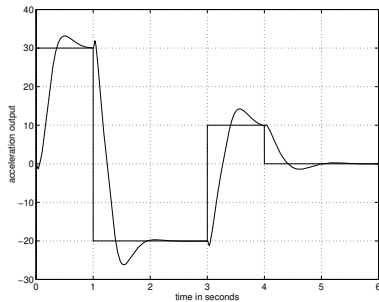


Convergence of the unperturbed motions

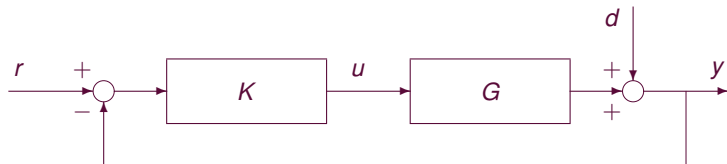
Constant (periodic) input



Constant (periodic) output



Disturbance attenuation of a set of perturbation d , for any initial condition



for d such that $\|W_p^{-1}(d)\|_{2,T} \leq \|d\|_{2,T} \Rightarrow \|y\|_{2,T} \leq \alpha$

The incremental norm as a rigorous extension of the H_∞ norm

Given an (augmented) nonlinear plant P_{NL}

$$\begin{cases} \dot{x}(t) &= f(x(t), w(t), u(t)) \\ z(t) &= g(x(t), w(t), u(t)) \\ y(t) &= h(x(t), w(t)) \end{cases}$$

Compute a nonlinear controller K_{NL}

$$\begin{cases} \dot{\bar{x}}(t) &= f_K(\bar{x}(t), y(t)) \\ u(t) &= g_K(\bar{x}(t), y(t)) \end{cases}$$

Such that the **incremental** \mathcal{L}_2 gain of the closed loop system is less than 1:
for all w_1, w_2

$$\forall T > 0, \int_0^T (z_1(t) - z_2(t))^T (z_1(t) - z_2(t)) dt < \int_0^T (w_1(t) - w_2(t))^T (w_1(t) - w_2(t)) dt$$

- As for \mathcal{L}_2 gain control, no efficient direct method for solving this problem

NL Plant

$$y = G_{NL}(u) : \begin{cases} \dot{x}(t) = f(x(t), u(t)) \\ y(t) = g(x(t), u(t)) \end{cases} \quad (1)$$



(Gâteaux Derivative) TV Linearizations of G_{NL} at $u_r \in \mathcal{L}_2$

$$\bar{y} = DG_{NL}[u_r](\bar{u}) : \begin{cases} \dot{\bar{x}}(t) = \bar{A}(t)\bar{x}(t) + \bar{B}(t)\bar{u}(t) \\ \bar{y}(t) = \bar{C}(t)\bar{x}(t) + \bar{D}(t)\bar{u}(t) \end{cases}$$

with

$$\begin{bmatrix} \bar{A}(t) & \bar{B}(t) \\ \bar{C}(t) & \bar{D}(t) \end{bmatrix} = \begin{bmatrix} \frac{\partial f}{\partial x}(x_r(t), u_r(t)) & \frac{\partial f}{\partial u}(x_r(t), u_r(t)) \\ \frac{\partial g}{\partial x}(x_r(t), u_r(t)) & \frac{\partial g}{\partial u}(x_r(t), u_r(t)) \end{bmatrix}$$

where $x_r(t)$ is the solution of (1) for the input $u(t) \equiv u_r(t)$

NL Plant

$$y = G_{NL}(u) : \begin{cases} \dot{x}(t) = f(x(t), u(t)) \\ y(t) = g(x(t), u(t)) \end{cases} \quad (1)$$



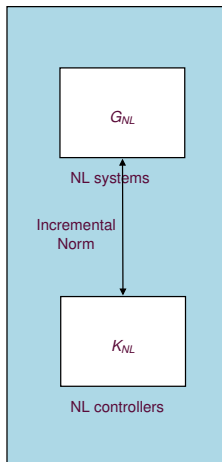
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Mean Value Theorem in Norm

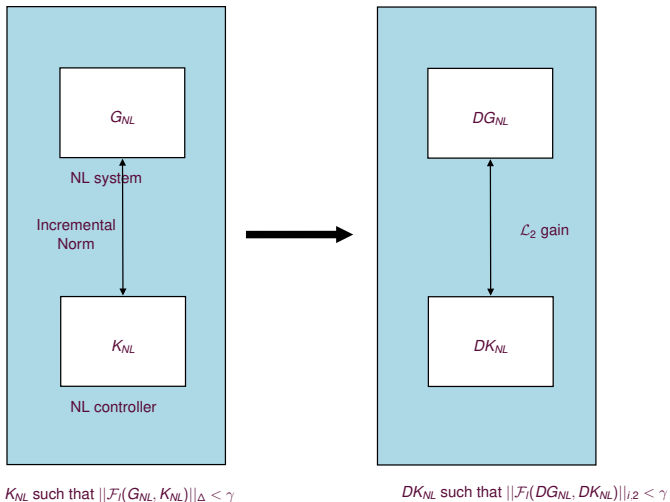
$$\|G_{NL}\|_{\Delta} \leq \gamma \quad \Leftrightarrow \quad \|DG_{NL}[u_r]\|_{i,2} \leq \gamma, \quad \forall u_r \in \mathcal{L}_2$$

An LPV approach for incremental synthesis



K_{NL} such that $\|\mathcal{F}_l(G_{NL}, K_{NL})\|_{\Delta} < \gamma$

An LPV approach for incremental synthesis



1 How to compute for any $u_r \in \mathcal{L}_2$, $DK_{NL}[u_r]$?

↔ Use an LPV method with G_{LPV} which embeds $DG_{NL}[u_r]$ for any u_r

2 From $DK_{NL}[u_r]$, defined for any $u_r \in \mathcal{L}_2$, how to compute K_{NL} ?

↔ focus on a special class of nonlinear control problems with the appropriated LPV control method

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↔ focus on a special class of nonlinear control problems with the appropriated LPV control method

To the time varying linearizations $DP_{NL}[w_r, u_r]$

$$\begin{cases} \dot{\bar{x}}(t) &= A(t)\bar{x}(t) &+ B_w(t)\bar{w}(t) &+ B_u(t)\bar{u}(t) \\ \dot{\bar{z}}(t) &= C_z(t)\bar{x}(t) &+ D_{zw}(t)\bar{w}(t) &+ D_{zu}(t)\bar{u}(t) \\ \dot{\bar{y}}(t) &= C_y(t)\bar{x}(t) &+ D_{yw}(t)\bar{w}(t) &+ D_{yu}(t)\bar{u}(t) \end{cases} \quad (3)$$

is associated an LPV plant

$$\begin{cases} \dot{x}(t) &= \mathbf{A}(\theta(t))x(t) &+ \mathbf{B}_1(\theta(t))w(t) &+ \mathbf{B}_2(\theta(t))u(t) \\ z(t) &= \mathbf{C}_1(\theta(t))x(t) &+ \mathbf{D}_{11}(\theta(t))w(t) &+ \mathbf{D}_{12}(\theta(t))u(t) \\ y(t) &= \mathbf{C}_2(\theta(t))x(t) &+ \mathbf{D}_{21}(\theta(t))w(t) &+ \mathbf{D}_{22}(\theta(t))u(t) \end{cases} \quad (4)$$

such that with

$$\Omega_{DNL} = \{ (\bar{x} \quad \bar{z} \quad \bar{y} \quad \bar{w} \quad \bar{u}) \mid \exists u_r, w_r, (3) \text{ is satisfied} \}$$

and

$$\Omega_{LPV} = \{ (x \quad z \quad y \quad w \quad u) \mid (4) \text{ is satisfied} \}$$

we have

$$\Omega_{DNL} \subset \Omega_{LPV}$$

- Roughly speaking, nonlinear system of the form

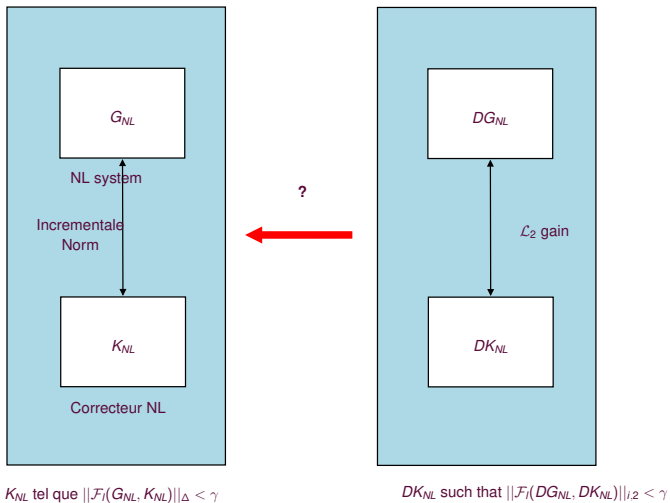
$$\begin{cases} \dot{x}(t) &= Ax(t) + B_2u(t) + \tilde{f}(x(t)) \\ x(0) &= x_0 \end{cases}$$

- with $\tilde{f}(x(t)) = B_0p(t)$
- where $p(t)$ is measured on-line or where the components of $x(t)$, $w(t)$ and $u(t)$ necessary for the computation of $p(t)$ are measured, that is, there exists a function α such that

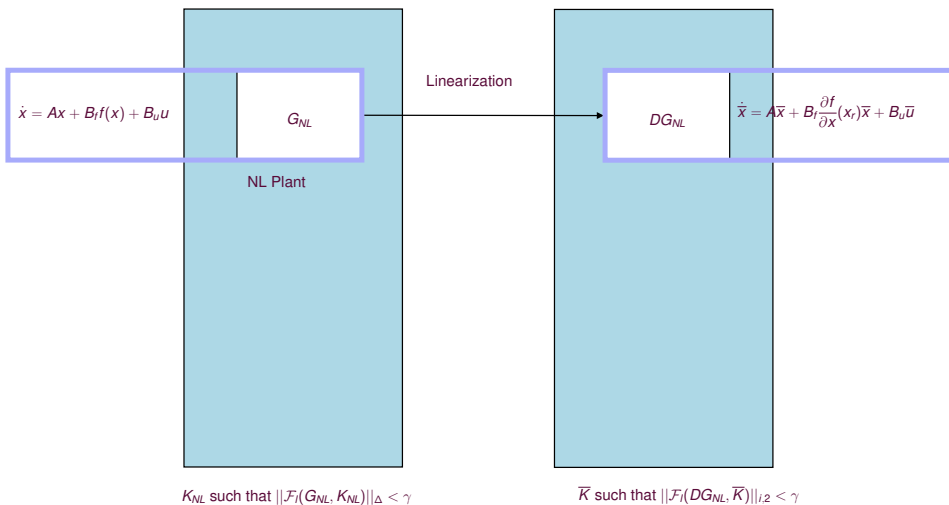
$$p(t) = \alpha(x(t), w(t), u(t))$$

- More details in S. de Hillerin, G. Scorletti, and V. Fromion, “Reduced-Complexity Controllers for LPV Systems: Towards Incremental Synthesis,” *Proc. IEEE Conf. on Decision and Control*, dec 2011

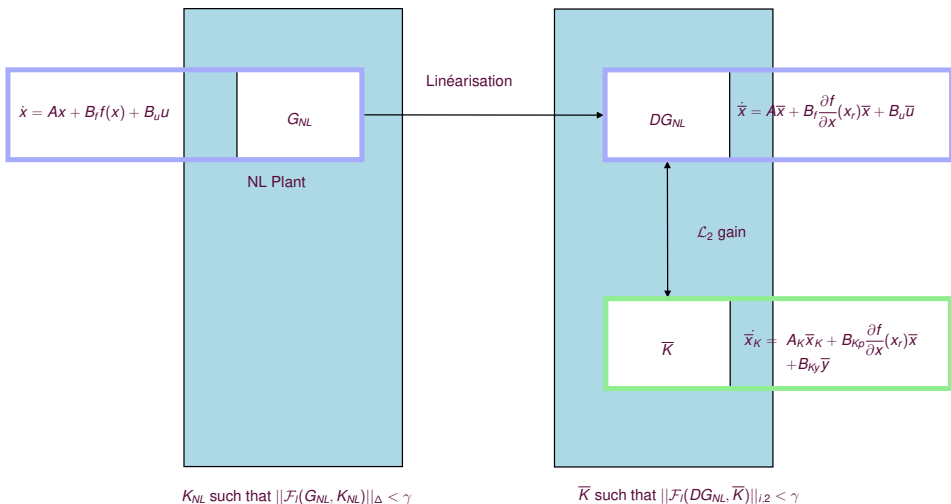
An LPV approach for incremental synthesis



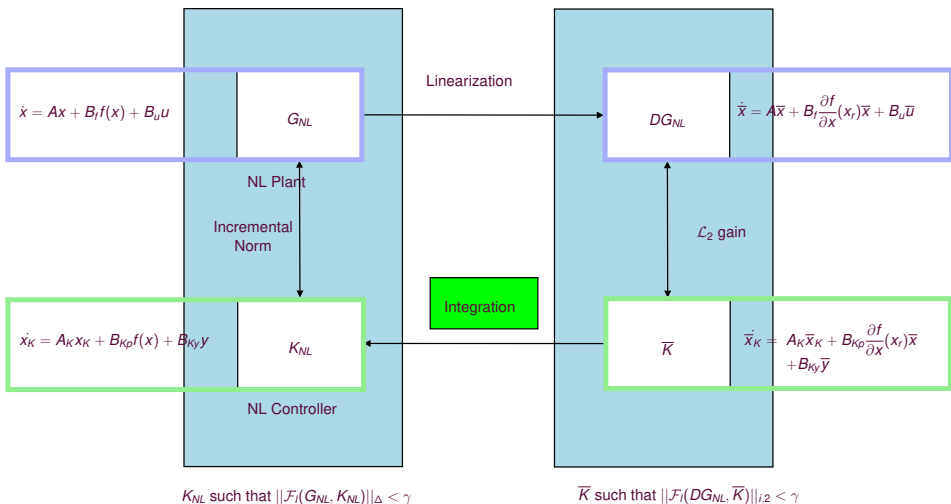
An LPV approach for incremental synthesis



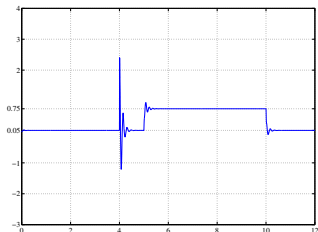
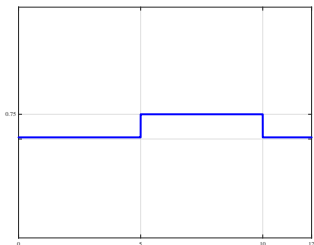
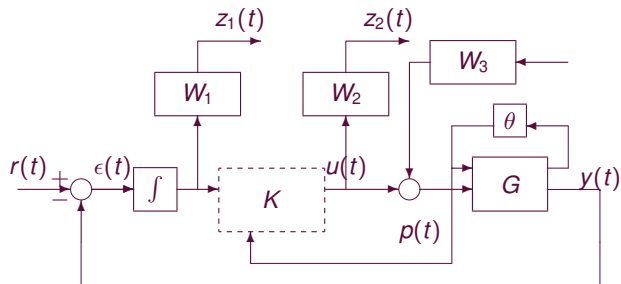
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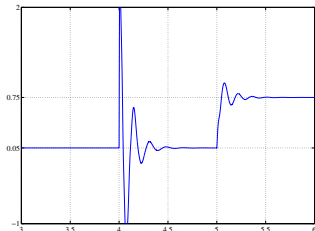
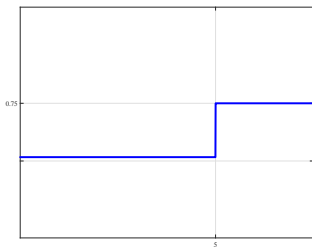
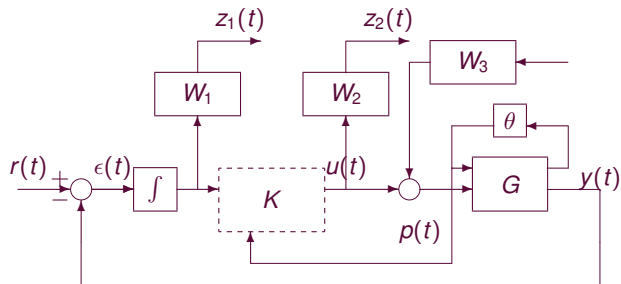


Application to the illustrative example: non-linear case



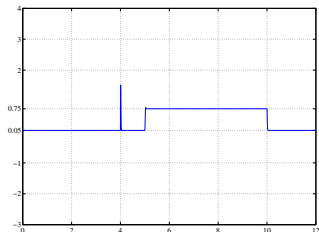
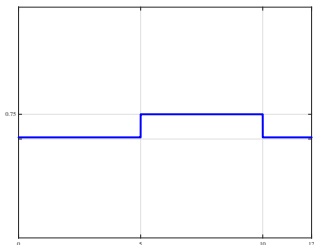
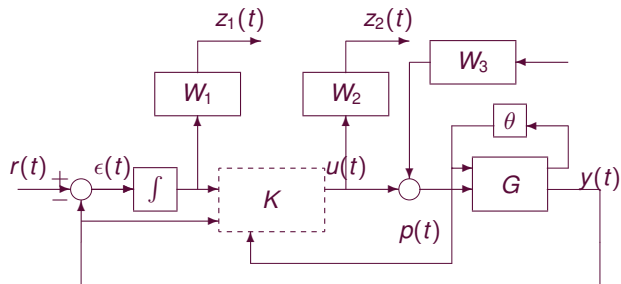
Tracking and rejection specs are satisfied.

Application to the illustrative example: non-linear case



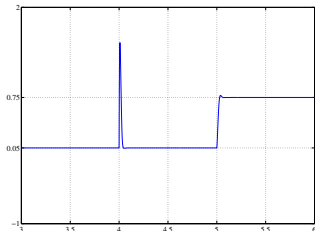
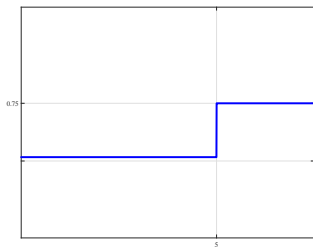
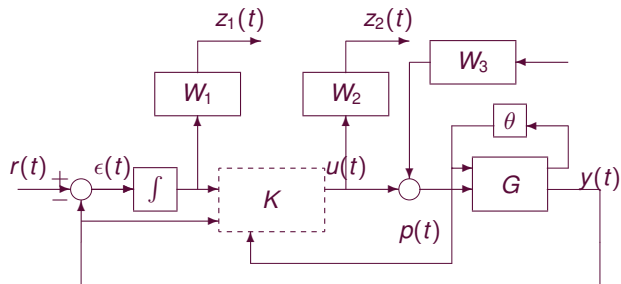
Tracking and rejection specs are satisfied.

Application to the illustrative example: non-linear case



Tracking and rejection specs are satisfied.

Application to the illustrative example: non-linear case



Tracking and rejection specs are satisfied.

- Two existing approaches of nonlinear control using LPV
 - Gain scheduling
 - Main idea: LPV model embeds **time invariant linearizations** of nonlinear plant
 - Interest: improve a widespread engineering practise
 - Drawback: few guarantees on the closed loop behavior
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- Pave the way to a common LTI/NL framework for performance control, ensuring typical closed-loop specifications
- A key result of robust control is the translation of performance specs in a well-posed optimisation problem (H_∞ norm, LTI case)
- Its extension for typical specs is not the \mathcal{L}_2 gain / stability approach but the incremental \mathcal{L}_2 gain / incremental stability one
- Combined with LPV methods, pave the way to the practical design of nonlinear controllers ensuring typical specifications
- Objective: propose a rigorous alternative to the widespread gain-scheduling control used by the engineers